

Integrating Data and Modeling In Materials Design

Ying CHEN¹, Yasunori KANETA¹, Shuichi IWATA²

¹ School of Engineering, The University of Tokyo, Japan

² Frontier Science, The University of Tokyo, Japan

Outline

I. Introduction: materials design

II. Approach

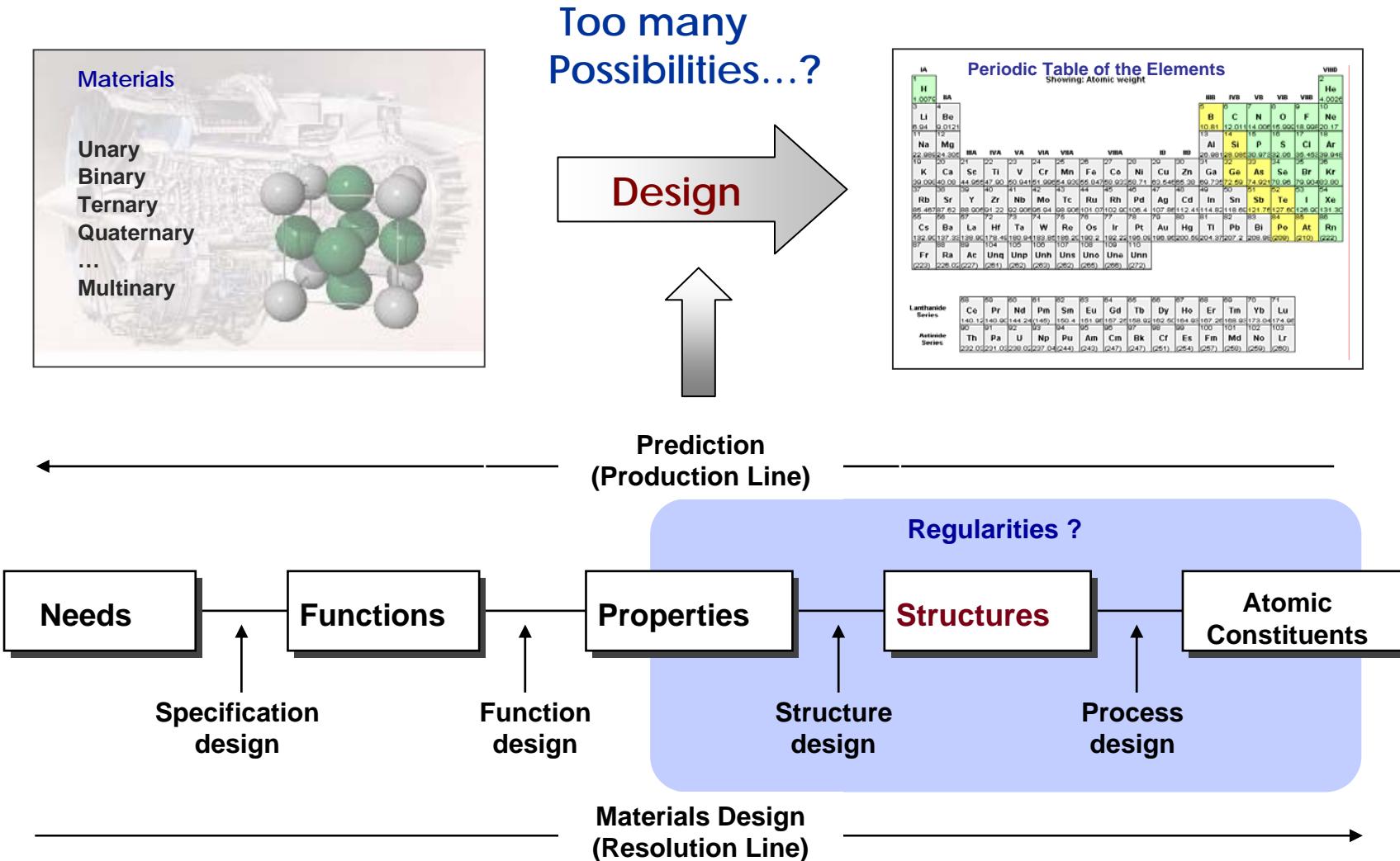
- Data-driven approach: data mining
- Modeling-driven approaches
- Data/Modeling-driven approach

III. Examples

- Structural map: empirical, computational
- Discovery of new H-storage materials
- 1st principles calculation of phase diagram

IV. Summary

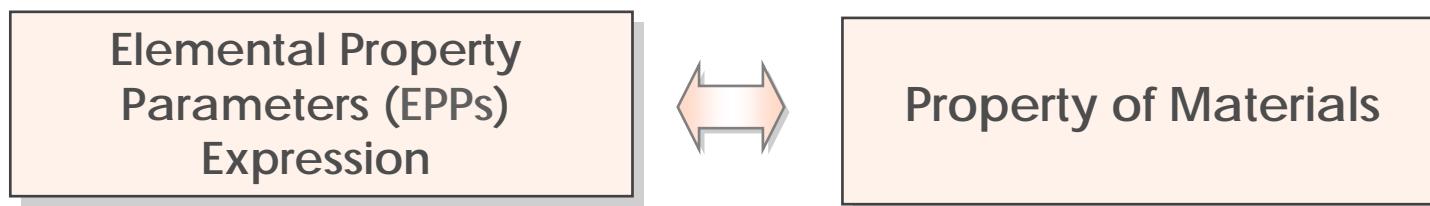
I. Introduction: Materials Design



II. Approaches: Data-Driven Approach

Basic Idea

- Based on the comprehensive materials database to reveal regularities:
 - Formation of compound in a given binary system
 - Composition of stable compounds in “compound formers”
 - Structures of a given compound
 - Properties of a given compound
- Postulation



- Tool: Materials Databases: Pauling File

II. Approaches: Data-Driven Approach

Mapping

- Purpose of Mapping

Proper Elemental Properties as Axes

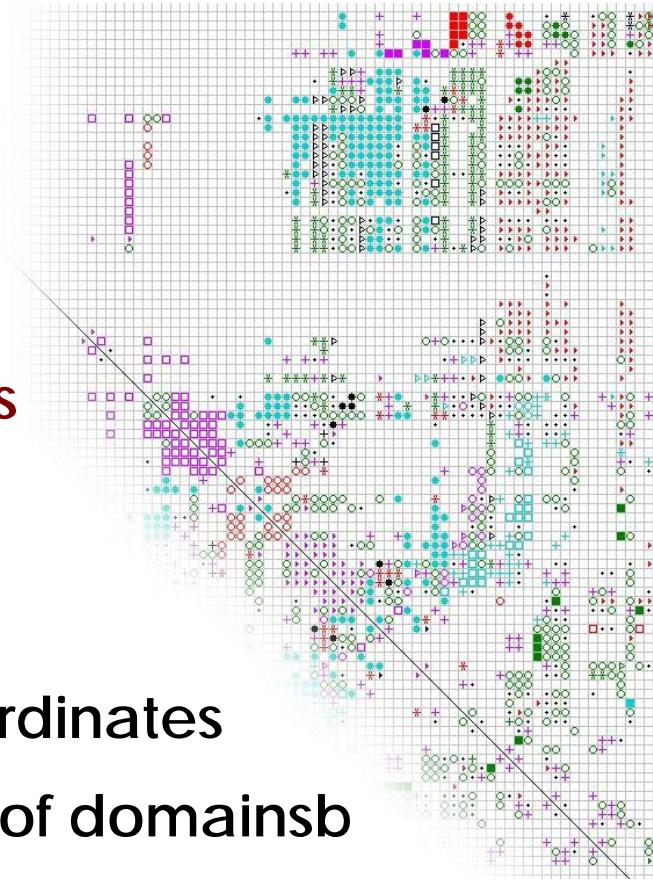


Substances in same/similar
structure/properties → Groups

- Two key points in mapping

Characterization: To find optimal coordinates

Classification: To define meaning of domains



II. Approaches: Modeling-Driven Approach

Calculations based on various physical models provide:

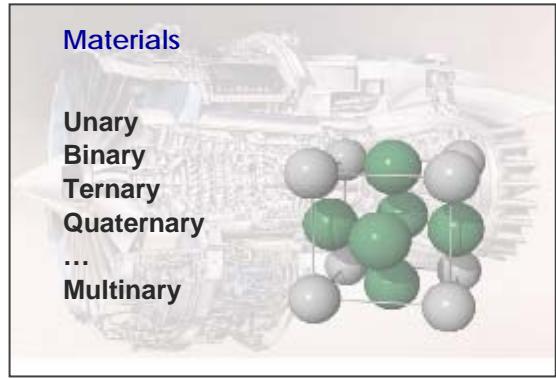
- Complement to empirical data, provide new data;
- Further screening and prediction of hypothesis;
- Understanding of insight into the origin;
- Prediction of materials with required properties.

II. Approaches: Modeling-Driven Approach

Theoretical Approaches

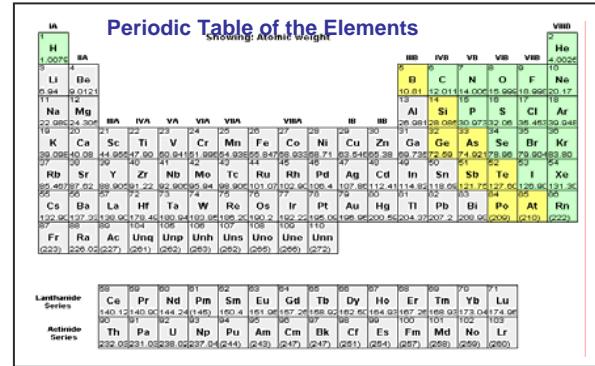
- First Principles Electronic Structures (FLAPW, Wien)
- Car-Parrinello Molecular Dynamics (CPMD, VASP)
- Cluster Expansion Method (CEM)
- Cluster Variation Method (CVM)
- Phase Field Method (PPM)
- Classical Molecular Dynamics (MD)
-

II. Approaches: Data/Modeling-Driven Approach

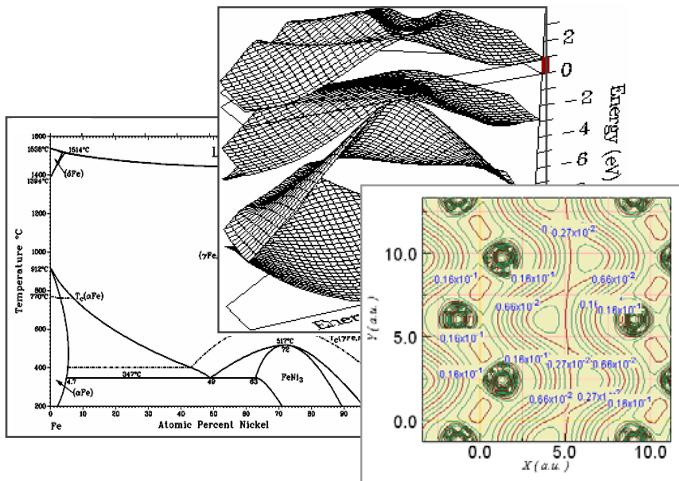


Too many
Possibilities...?

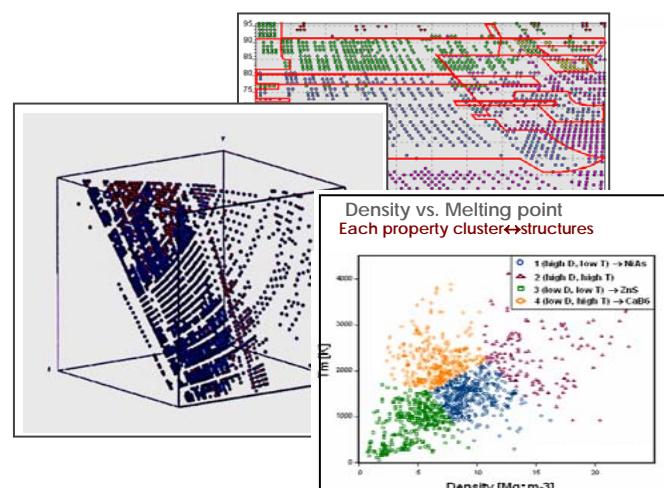
Design



Regularities



Model-Driven Approach → Origin



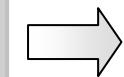
Data-Drive Approach → Discovery

III. Example-1 Structural Map

Strategy

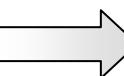
Purpose: Regularity between Crystal structure & Element properties

Optimal coordinates
56
Element Property
Parameters



- 6 most distinct EPP groups

Group number
Mendeleev number
Cohesion energy
Electrochemical factor
Size



- Operations

Sum $EP(A) + E$

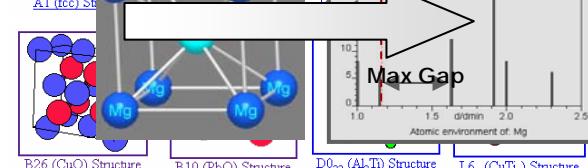
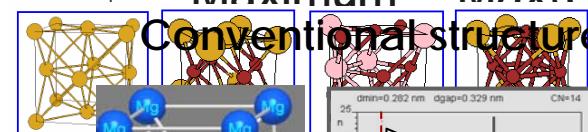
Difference $EP(A) - E$

Product $EP(A) * E$

Ratio $EP(A) / EP(B)$

Maximum $\text{Max}(EP(A), EP(B))$

Conventional structure types



2-3
Optimal EPP
Expressions

Distribution,
Patterns, 😊

~30
Local Environment
Types

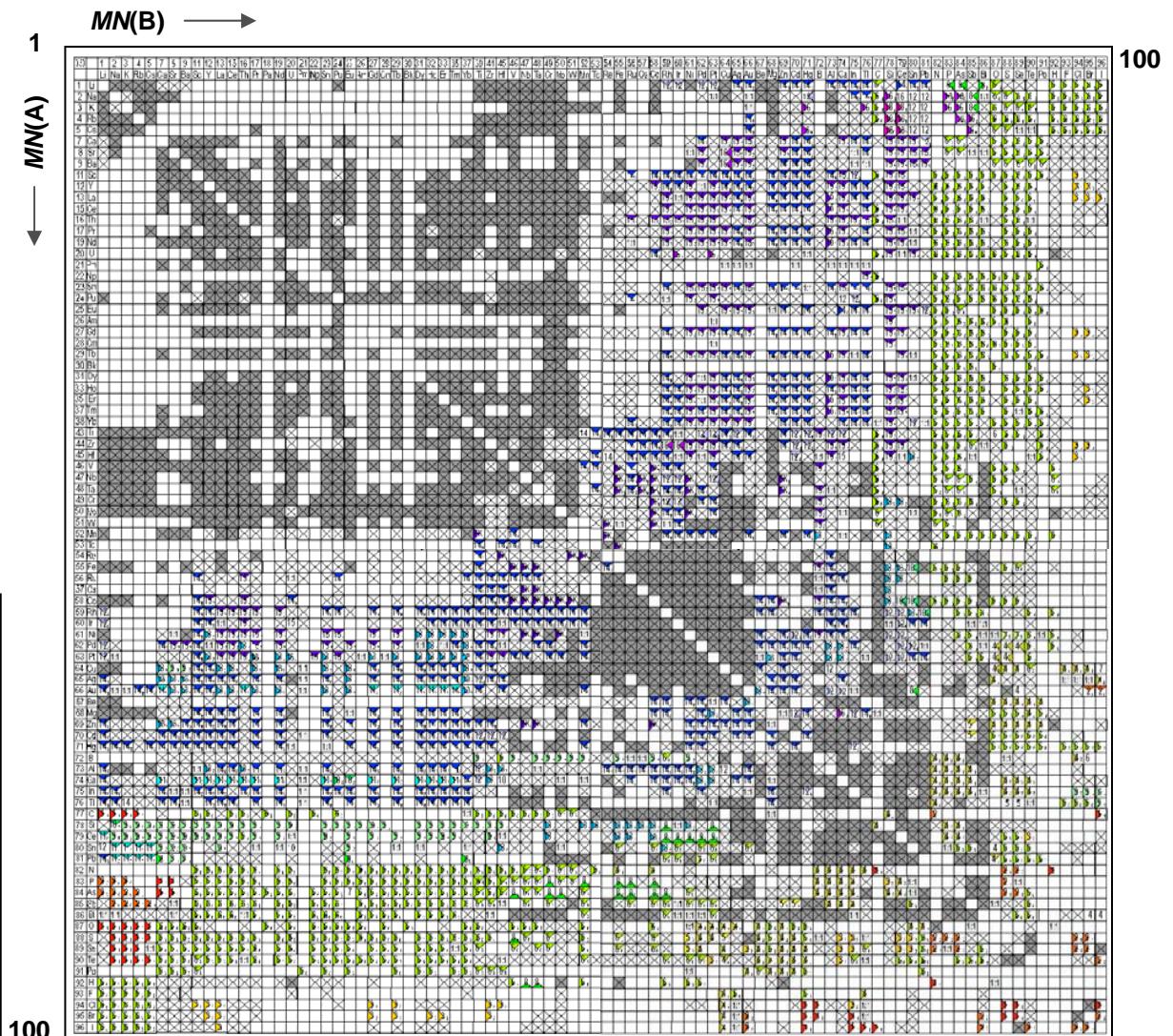
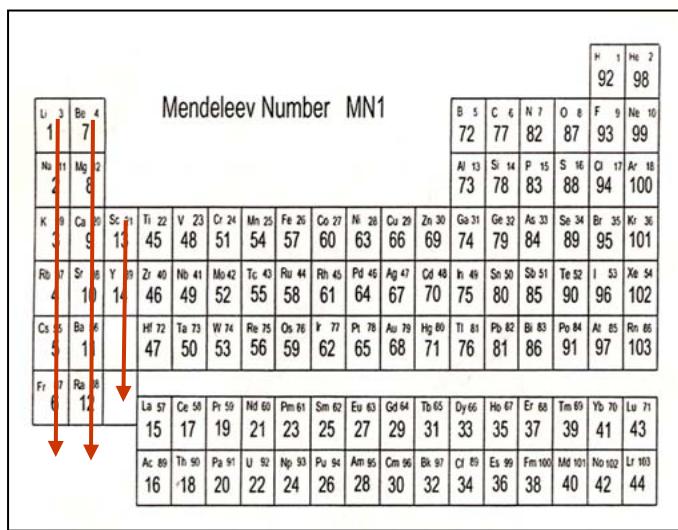
Definition of domains
~3,500
Conventional
Structures Types

III-1 Empirical Structure Map

Mendeleev Number

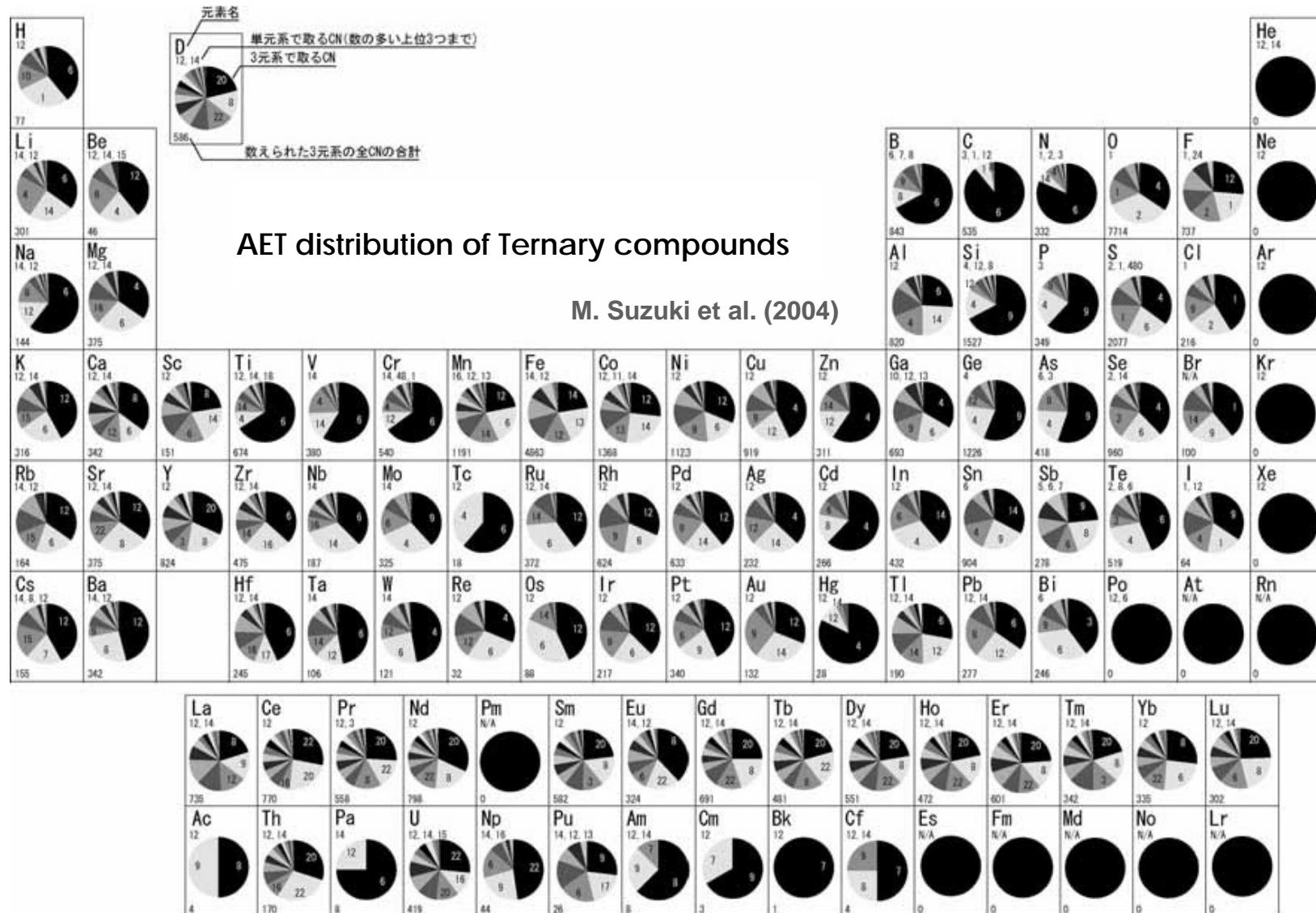
$MN(A)$ vs. $MN(B)$
Map for 1:1
Binary
Compounds (RT)

- CN 1-3
- CN
- CN 6 (-11)
- CN 12 (-13)
- CN 14(-18)
- Non-former
- ☒ Former (no 1:1)



P. Villars, Y. Chen et al. (2004)

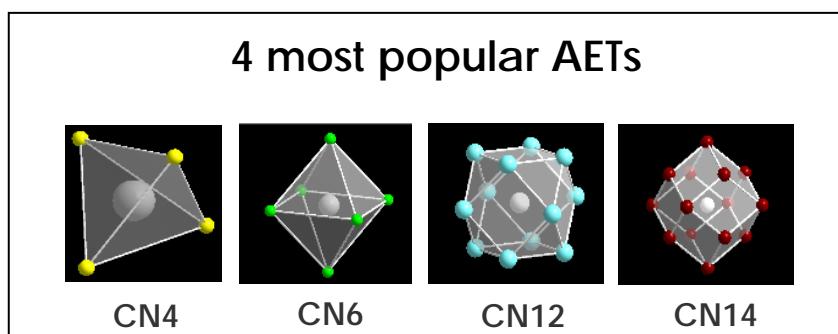
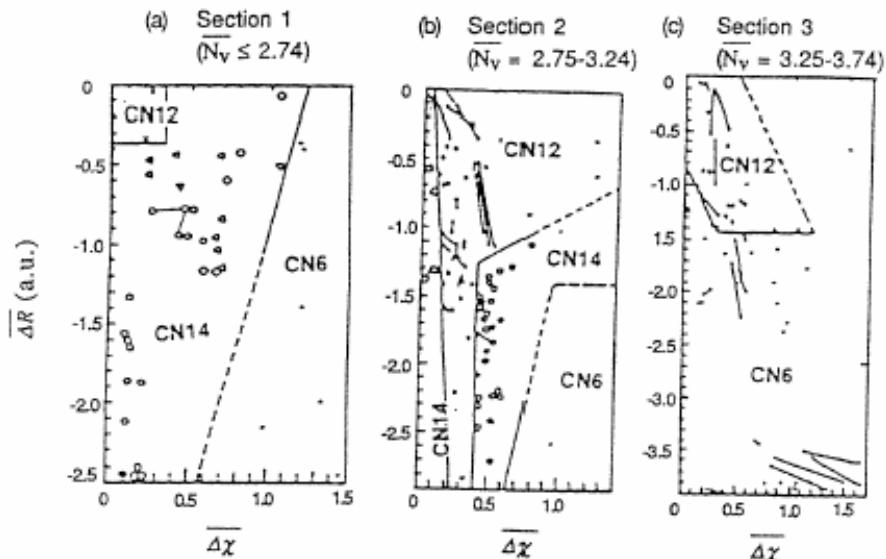
III-1 AET distribution of Ternary compounds



III-1 Empirical Structure Map

3 physical ordinates

Successfully separated ~2,500 intermetallic compounds with single AET



P. Villars et al. (1983)

x: difference of Zunger's radii
y: difference of M-B elentronegativity
z: sum of valence electrons number

Problems

- Microscopic mechanism ?
- Uncompleted separation



Theoretical Modeling:
Calculated map

III-1 Calculated Structural Map for AET Model, Method

Model Systems

AB intermetallic compound

- Nv < 3.5, s-s, s-p, p-d
- Martynov-Batsanov's electronegativity χ

$$\overline{\Delta\chi} = \chi_A - \chi_B$$

→ Atomic valence electronic energy level $\{\varepsilon_i\}$

$$\Delta E = E_A - E_B$$

- Pseudopotential radii's sum $R = r_s + r_p$

→ Bond length d

Calculation Approaches

Tight-binding approach

$$E_{tot} = E_{bond} + E_{rep}$$

E_{bond} - attractive bond energy: $E_{bond} = \sum_k^{occ.} q_k \varepsilon_k$

$$H = \sum_{i\alpha} \varepsilon_{i\alpha} |i\alpha\rangle\langle i\alpha| + \sum_{ij\beta} h_{ij\beta} |i\alpha\rangle\langle j\beta| + |j\beta\rangle\langle i\alpha|$$

$$h_{\alpha\beta\gamma}(d) = \eta_{\alpha\beta\gamma} \frac{h}{md^2}$$

E_{rep} - pairwise repulsive contribution

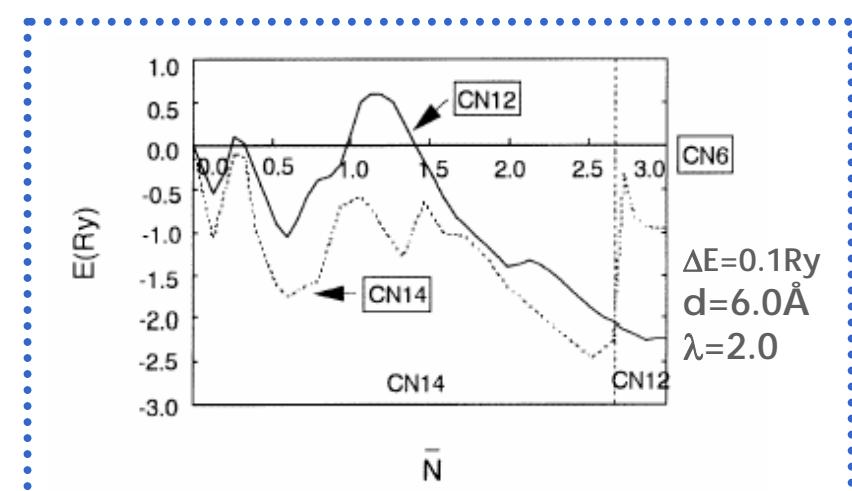
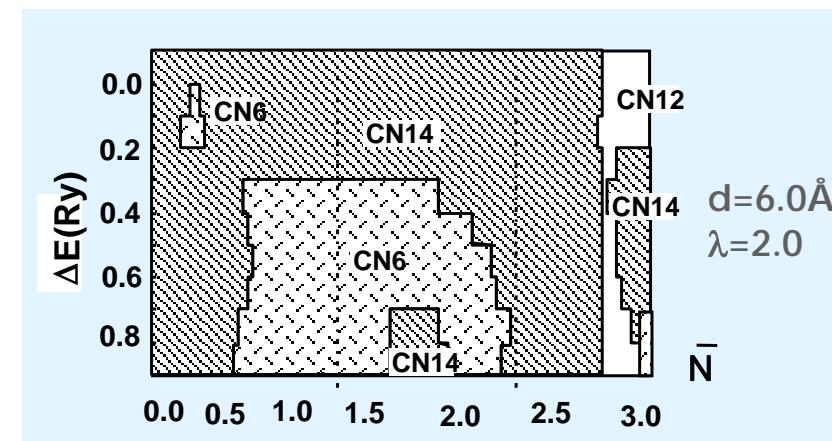
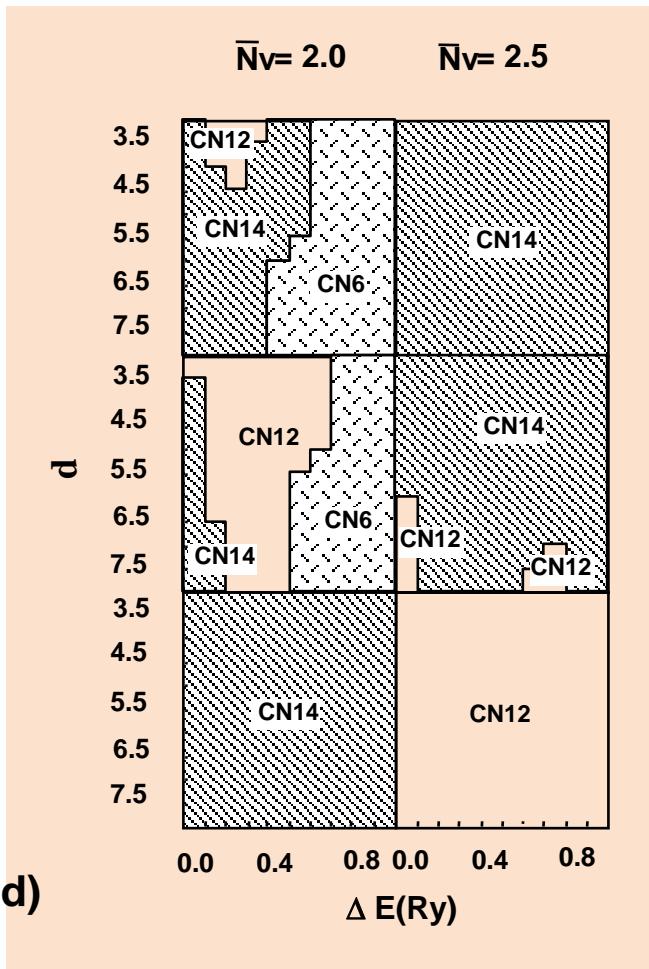
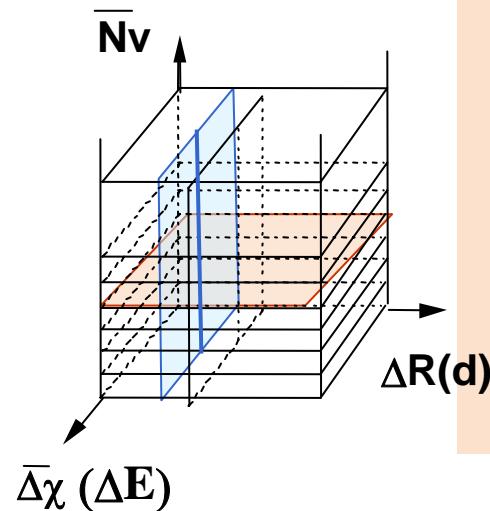
$$E_{rep} = \frac{1}{2N} \sum_{i,j} \Phi(R_{ij}) \quad \Phi_{AA}(\mathbf{R}) = \mathbf{h}^\lambda(\mathbf{R})$$

Structural energy difference theorem

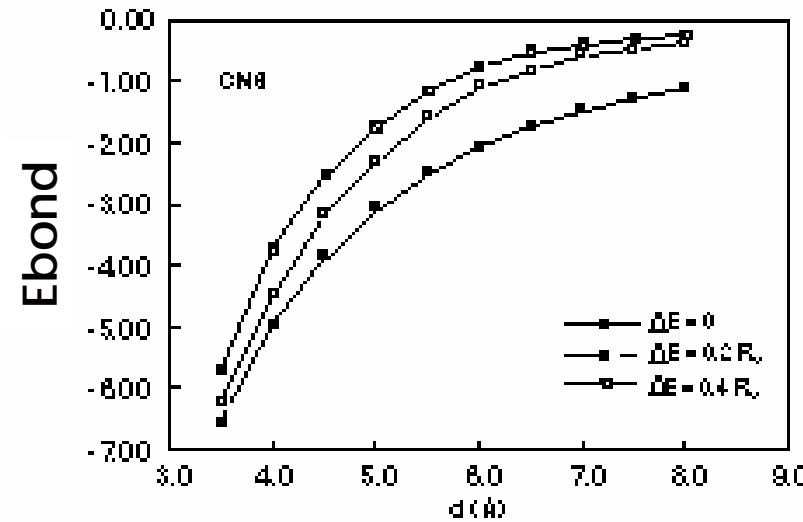
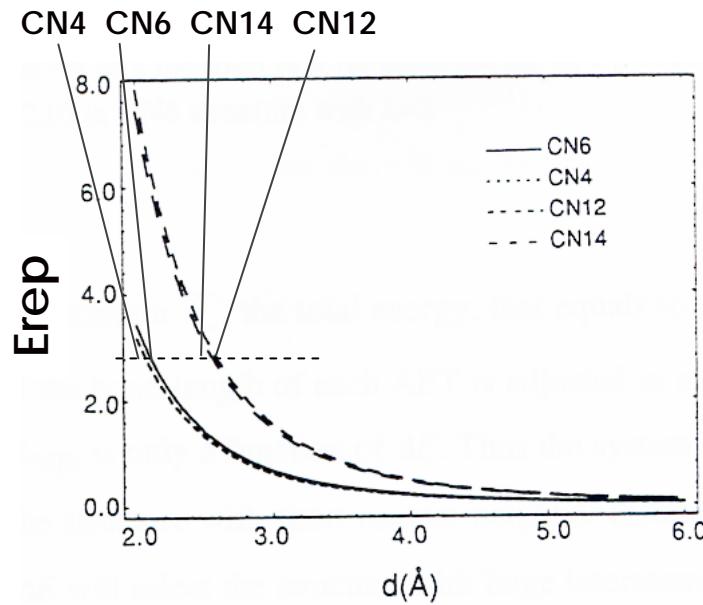
$$\Delta E_{tot} = (\Delta E_{bond})_{\Delta E_{rep}=0}$$

III-1 Calculated Structural Map for AET

Results



Investigate Origin of structural preference



Influence of ΔE : large $\Delta E \rightarrow$ small $d \rightarrow$ CN4 and CN6
 \rightarrow CN4 requires very large ΔE , no in low Nv .

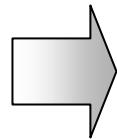
Influence of λ : higher $\lambda \rightarrow$ higher CN: CN12, CN14

III. Example-2: Discovery of New H-Storage Materials

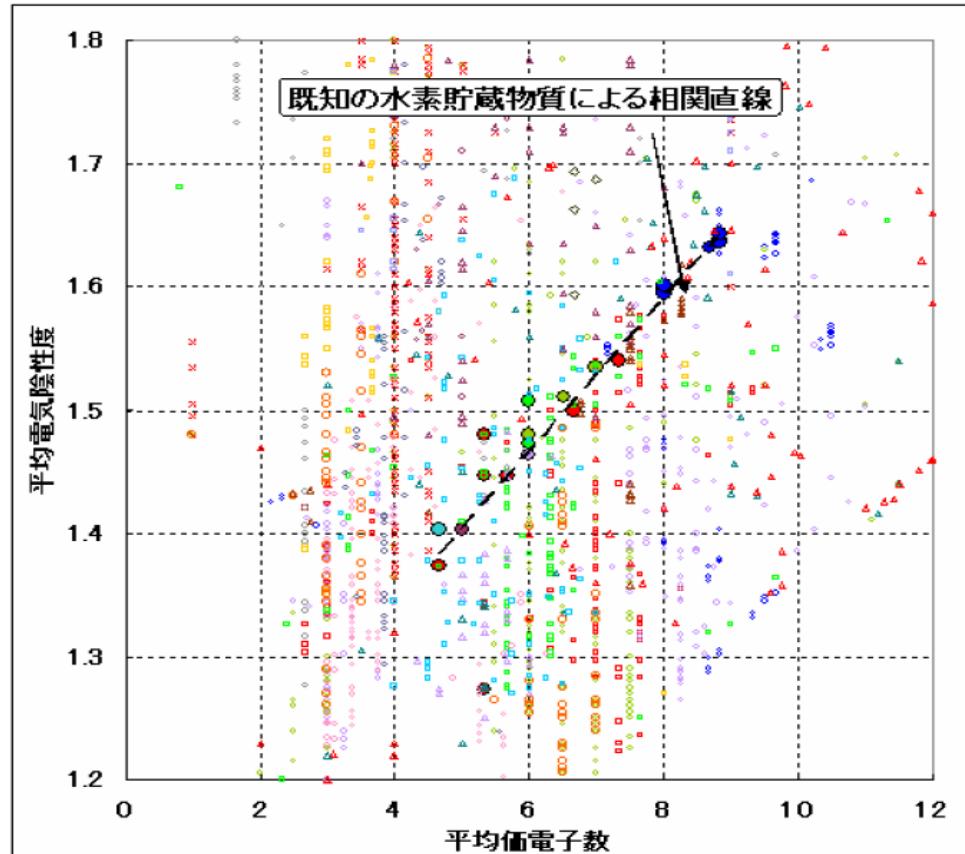
Starting point

32 Already known
H-storage alloys (HAS)

結晶構造	水素貯蔵物質
CaCu ₅	LaNi ₅ , LaCo ₅ , CaNi ₅ , CeCo ₅ , CeNi ₅ , GdCo ₅ , GdNi ₅ , NdCo ₅ , NdNi ₅ , PrCo ₅ , PrNi ₅ , YNi ₅ , YCo ₅ , ThCo ₅ , YbNi ₅ , SmNi ₅ , SmCo ₅
CsCl	TiFe, TiNi, TiCo
Mg ₂ Cu	Mg ₂ Cu
Mg ₂ Ni	Mg ₂ Ni
MgCu ₂	ZrV ₂ , ZrCo ₂ , ZrMo ₂ , ZrFe ₂ , ZrCr ₂ , TiCr ₂ , Ti ₂ Co
MgZn ₂	ZrMn ₂ , TiMn ₂
Ti ₂ Ni	Ti ₂ Ni



Surprising
linear relation for known HSAs
Average valence electrons
VS.
Average electronegativity



- CaCu₅ • CaCu₅-H • CsCl • CsCl-H • Mg₂Cu
- Mg₂Cu-H • Mg₂Ni • Mg₂Ni-H • MgCu₂ • MgCu₂-H
- MgZn₂ • MgZn₂-H • NaCl • Cu₃Au • Mn₅Si₃
- W • Mg • AlB₂ • Ti₂Ni • Ti₂Ni-H
- TlI • Th₃P₄ • CaF₂ • Cr₃Si • NiAs
- ZnS • FeS • PuNi₃

M. Ono et al. (2005)

III-2. Discovery of New H-Storage Materials

linear relation for known HSAs → Candidates of new HSAs

From small **distance** To the straight line

化学式	結晶構造	L	化学式	結晶構造	L
ErNi ₅	CaCu ₅ ,hP6,191	0.000	Nd ₅ Sb ₃	Mn ₅ Si ₃ ,hP16,193	0.001
ThNi ₅	CaCu ₅ ,hP6,191	0.000	Pr ₅ Sb ₃	Mn ₅ Si ₃ ,hP16,193	0.001
TmNi ₅	CaCu ₅ ,hP6,191	0.000	Sm ₅ Sb ₃	Mn ₅ Si ₃ ,hP16,193	0.001
TaFe ₂	MgZn ₂ ,hP12,194	0.000	Ce ₅ Sb ₃	Mn ₅ Si ₃ ,hP16,193	0.001
TaCo ₂	MgCu ₂ ,cF24,227	0.000	Yb ₅ Sb ₃	Mn ₅ Si ₃ ,hP16,193	0.001
La ₅ Si ₃	Mn ₅ Si ₃ ,hP16,193	0.000	HoFe ₅	CaCu ₅ ,hP6,191	0.001
NpFe ₂	MgCu ₂ ,cF24,227	0.001	Mn ₃ Rh	Cu ₃ Au,cP4,221	0.001
PuFe ₂	MgCu ₂ ,cF24,227	0.001	WFe ₂	MgZn ₂ ,hP12,194	0.001
UFe ₂	MgCu ₂ ,cF24,227	0.001	ScCo ₂	MgCu ₂ ,cF24,227	0.001
NdFe ₅	CaCu ₅ ,hP6,191	0.001	ErIn	CsCl,cP2,221	0.001
DyNi ₅	CaCu ₅ ,hP6,191	0.001	GdIn	CsCl,cP2,221	0.001
HoNi ₅	CaCu ₅ ,hP6,191	0.001	TmIn	CsCl,cP2,221	0.001
TbNi ₅	CaCu ₅ ,hP6,191	0.001	YIn	CsCl,cP2,221	0.001
HfMn ₂	MgZn ₂ ,hP12,194	0.001	LuNi ₅	CaCu ₅ ,hP6,191	0.001
CeBi	CsCl,cP2,221	0.001	Sc ₅ Pb ₃	Mn ₅ Si ₃ ,hP16,193	0.001
BaPo	NaCl,cF8,225	0.001	DyCo ₅	CaCu ₅ ,hP6,191	0.001
CeBi	NaCl,cF8,225	0.001	HoCo ₅	CaCu ₅ ,hP6,191	0.001
AmNi ₂	MgCu ₂ ,cF24,227	0.001	TbCo ₅	CaCu ₅ ,hP6,191	0.001
NpNi ₂	MgCu ₂ ,cF24,227	0.001	RuAl	CsCl,cP2,221	0.001
PuNi ₂	MgCu ₂ ,cF24,227	0.001	GdFe ₅	CaCu ₅ ,hP6,191	0.001
UNi ₂	MgZn ₂ ,hP12,194	0.001	ThFe ₅	CaCu ₅ ,hP6,191	0.001
NpCo ₂	MgCu ₂ ,cF24,227	0.001	ScFe ₂	MgCu ₂ ,cF24,227	0.001
PuCo ₂	MgCu ₂ ,cF24,227	0.001	ScFe ₂	MgZn ₂ ,hP12,194	0.001
UCo ₂	MgCu ₂ ,cF24,227	0.001			

Further screening by
large **unfilled volume**

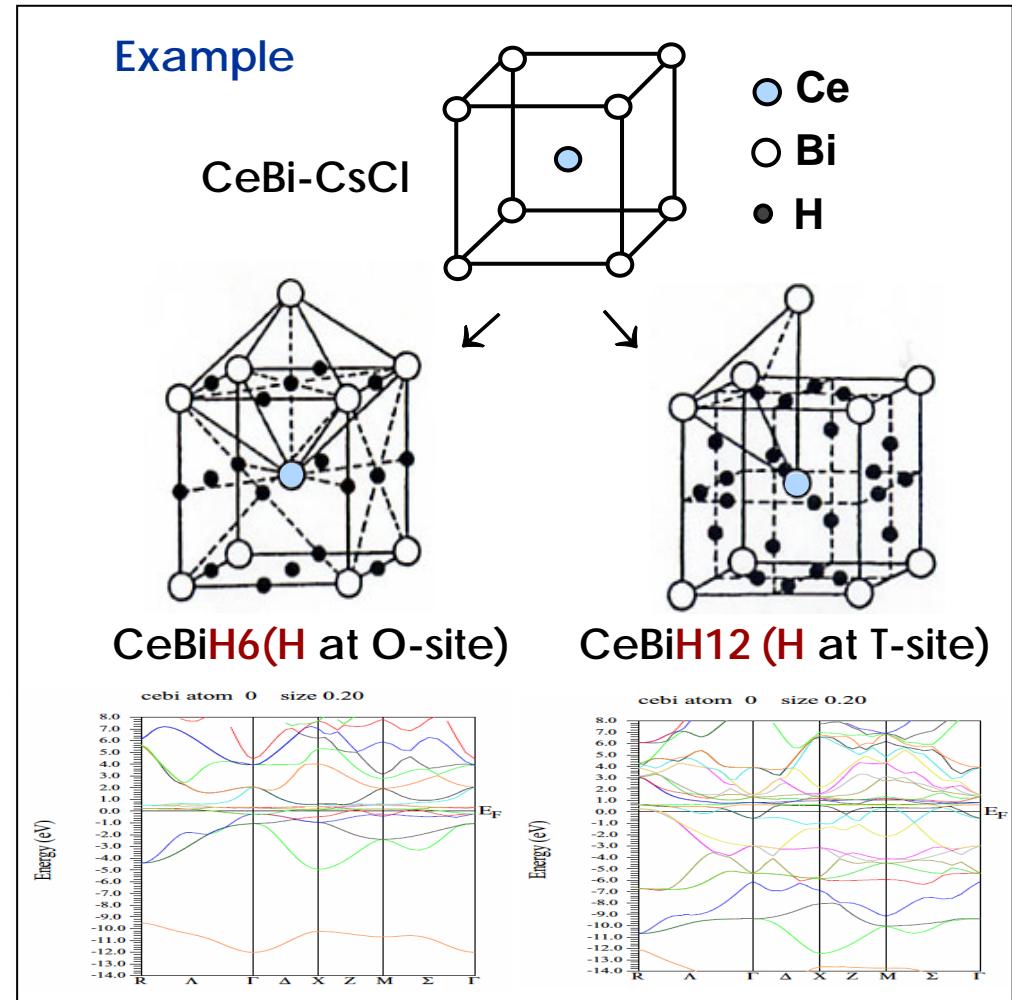
結晶構造	隙間の体積 [Å ³ Atom ⁻¹]	直線との 距離
PuCo ₃	PuNi ₃	4.36 0.0157
PuNi ₃	PuNi ₃	4.30 0.0120
ThFe ₃	PuNi ₃	4.12 0.0120
HfV ₂	MgCu ₂	4.37 0.0037
NpFe ₂	MgCu ₂	4.41 0.0108
NpNi ₂	MgCu ₂	4.25 0.0076
PuFe ₂	MgCu ₂	4.20 0.0120
PuNi ₂	MgCu ₂	4.23 0.0105

III-2. Discovery of New H-Storage Materials

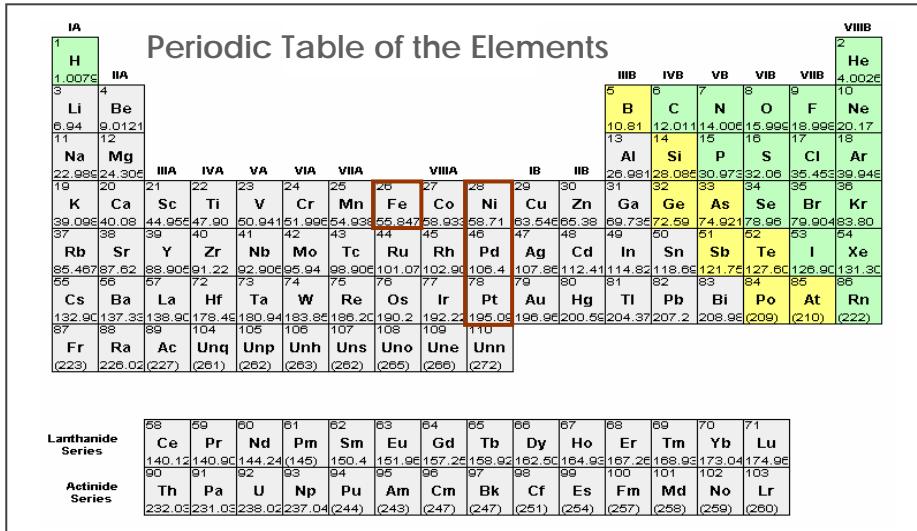
First Principles Calculation: A_nB_m , $A_nB_mH_q$

- Possible H sites, structures stability
- Interstitial volume, Storage capacity
- Electronic structure, binding
- Formation energy, Dissociation pressure

→ Candidates of New H-storage alloys !

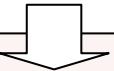


III-3 Phase Equilibrium of Fe-Pt, Pd, Ni



III. Example 3: First Principles Cal. of Phase Diagram

Atomic Information

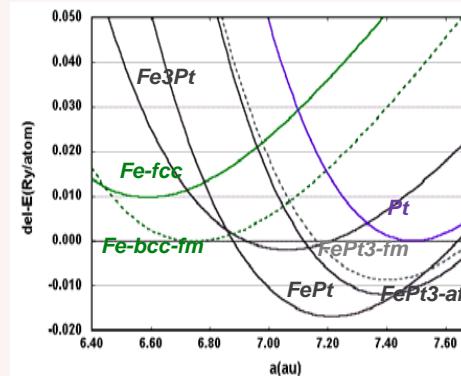


Internal Energy (First principles): E

Cluster Expansion Method (CEM)

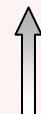
$$E^{(k)}(r) = \sum_{i=1}^m v_i(r) \cdot \xi_i^k$$

$$v_i = \sum_{k=0}^{m-1} \{\xi_j^k\}^{-1} \cdot E^{(k)}$$



Thermodynamics: $F = E - T \cdot S$

$$F(T, V(r), \{\xi_i\}) = \sum_j v_j(V(r), \{\xi_i\}, T) - T \cdot S(\{\xi_i\})$$



Cluster Variation Method (CVM): S

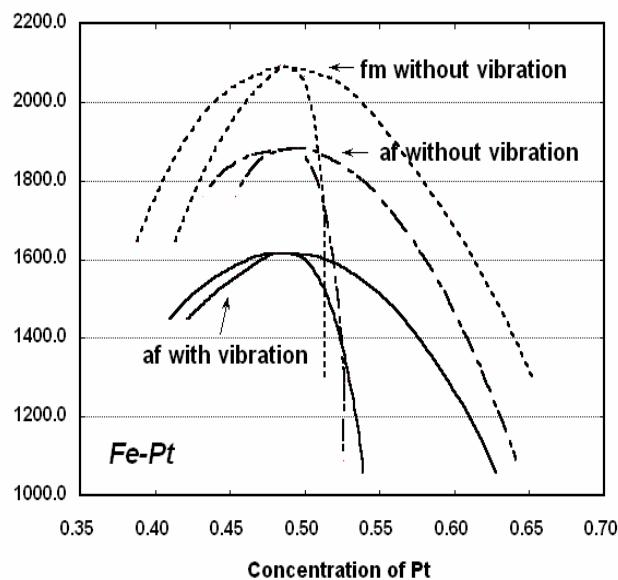
$$S = k_B \cdot \ln \frac{\prod_{i,j} \{N y_{ij}\}^6 \cdot \{N!\}}{\prod_i \{N x_i\}^5 \cdot \prod_{i,j,k,l} \{N w_{ijkl}\}^2}$$

Phase Equilibria, Thermo-dynamic properties

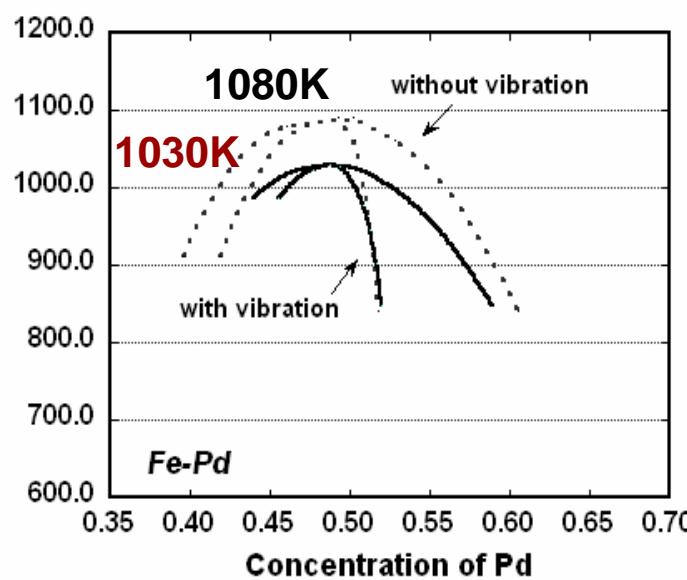
III-3 Phase Equilibrium of Fe-Pt, Pd, Ni

Phase Diagram: L10-disorder, Phase Separation

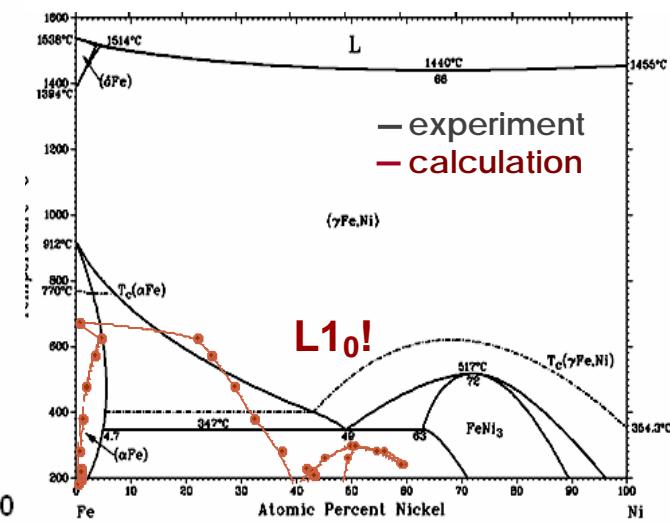
Fe-Pt



Fe-Pd



Fe-Ni



Experiment
1600K

Experiment
1023K

No L10 in exp. Phase diagram: Stable L10?
Exp.(1962), MC(1996): 590K~775K
Ohuma et al. ASM meeting 2004

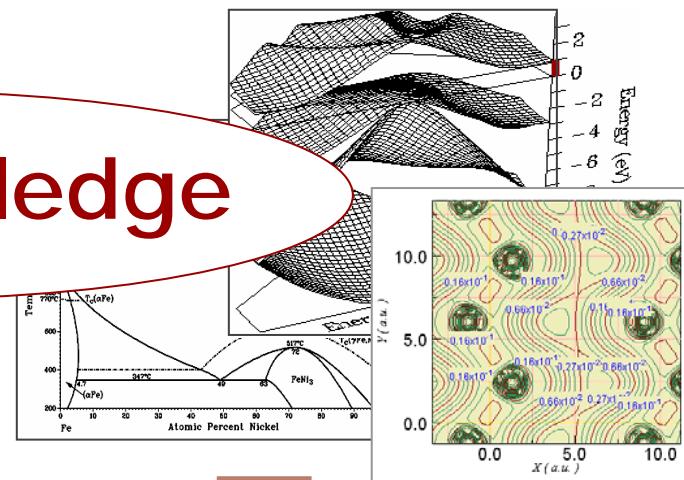
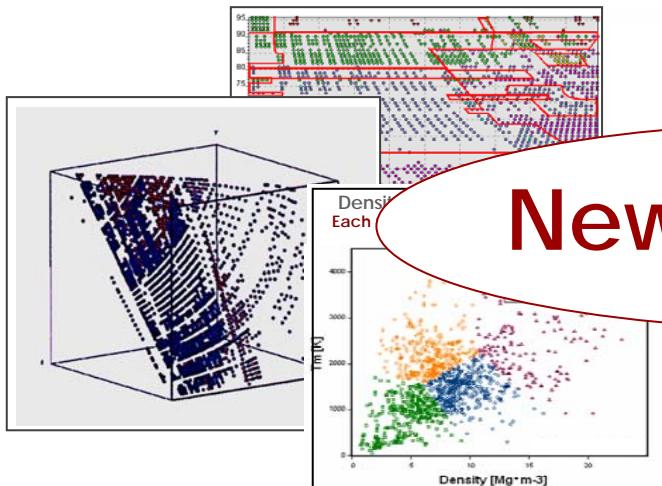
IV. Summary

Interaction of Data & Modeling

Data Mining
→ Regularity

Modeling
→ Physical Origin

New knowledge





Thank you very much !

II. Mapping Approach

Characterization

Element Properties (56 properties, ...182 data sets)

atomic number
atomic weight
density
molar volume
atomic energy level (Herman-Skillman)
valence electron number
atomic radius
Van der Waals radius
covalent radius
first ionic radius
second ionic radius
third ionic radius
metallic radius
Zunger pseudo-potential radius
Pauling electronegativity
Alfred-Rochow electronegativity
Martynov-Batsanov electronegativity
absolute electronegativity
first ionization energy
second ionization energy
third ionization energy
molar electronic affinity

Young's modulus
rigidity modulus
bulk modulus
Poisson's ratio
mineral hardness
Brinell hardness
melting temperature
Vickers hardness
boiling temperature
Debye temperature
thermal conductivity
molar heat capacity
coefficient of linear thermal expansion
atomization enthalpy
fusion enthalpy
vaporization enthalpy
electrical resistance
magnetic susceptibility
reflectivity
refractive index
...

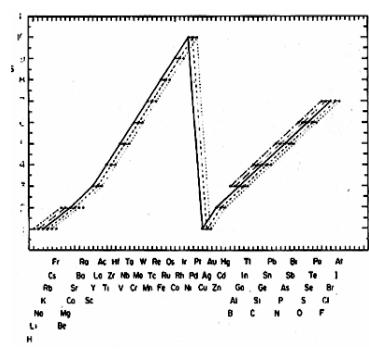
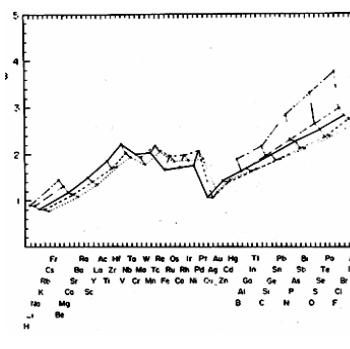
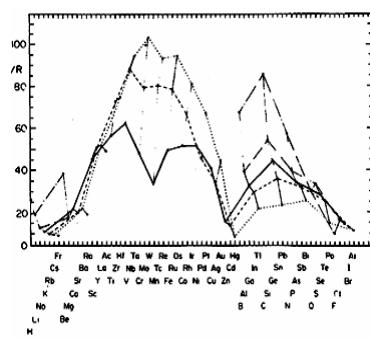
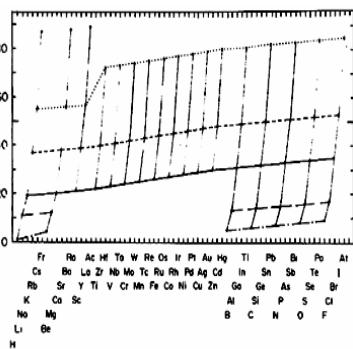
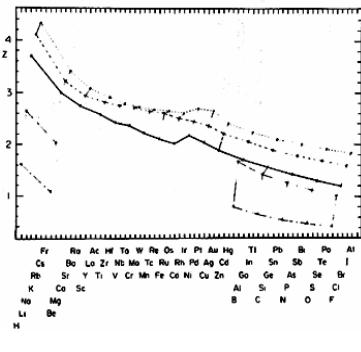
Optimal coordinate
for certain problem?

II. Mapping Approach

Characterization

Element property vs. Atomic number

- 5 Patterns
- 5 Element property groups
- 1 representative for 1 group



Size factor

**Atomic No.
factor**

**Cohensive
energy
factor**

**Electro-
chemical
factor**

**Valence
electron
factor**

Zunger's
pseudopotential
radii (r_s , r_p , ...)

Atomic No.

Atomization
energy

Electro-
negativity

valence
electron

II. Mapping Approach

Characterization

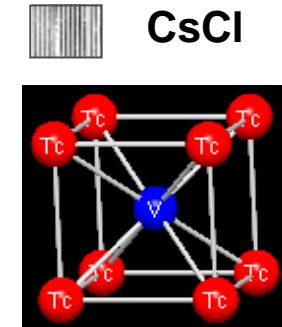
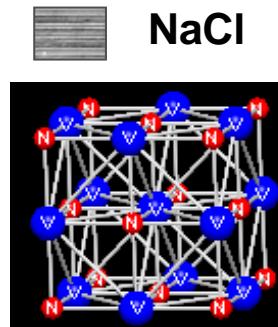
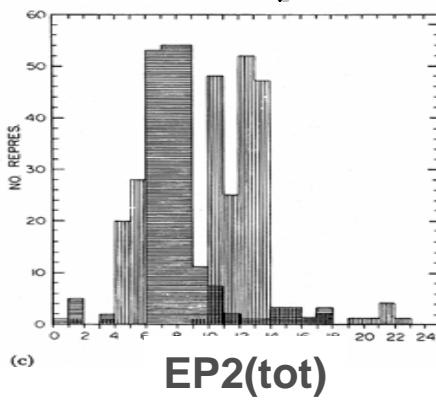
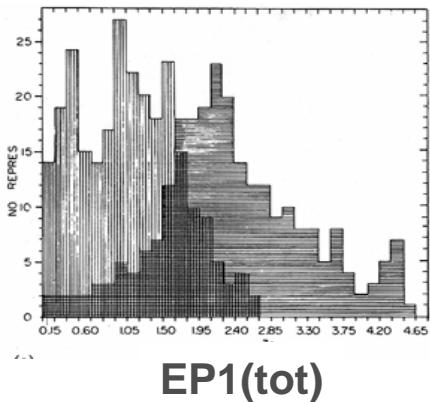
Expression of compound property by element property

$$EP(tot) = EP(A) \text{ op } EP(B)$$

Operations

Sum	$EP(A)+EP(B)$
Difference	$EP(A)-EP(B)$
Product	$EP(A)*EP(B)$
Ratio	$EP(A)/EP(B)$
Maximum	$\text{Max}(EP(A),EP(B))$
Minimum	$\text{Min}(EP(A),EP(B))$

Test separating capacity
for NaCl-type and CsCl-type structures



II. Mapping Approach

Classification

31 Most common Atomic Environment Types (AETs)

